

TRIGONOMETRY (Q 4 & 5, PAPER 2)

LESSON NO. 6: SUMS & PRODUCTS

2006

4 (b) (i) Express $\sin(3x + 60^\circ) - \sin x$ as a product of sine and cosine.

SOLUTION

4 (b) (i)

$$\begin{aligned}\sin(3x + 60^\circ) - \sin x &= 2 \cos\left(\frac{4x + 60^\circ}{2}\right) \sin\left(\frac{2x + 60^\circ}{2}\right) \\ &= 2 \cos(2x + 30^\circ) \sin(x + 30^\circ)\end{aligned}$$

SUMS \rightarrow PRODUCTS

$$\sin A + \sin B = 2 \sin\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$$

$$\sin A - \sin B = 2 \cos\left(\frac{A+B}{2}\right) \sin\left(\frac{A-B}{2}\right)$$

$$\cos A + \cos B = 2 \cos\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$$

$$\cos A - \cos B = -2 \sin\left(\frac{A+B}{2}\right) \sin\left(\frac{A-B}{2}\right)$$