

SAMPLE PAPER 5: PAPER 1

QUESTION 2 (25 MARKS)

Question 2 (a)

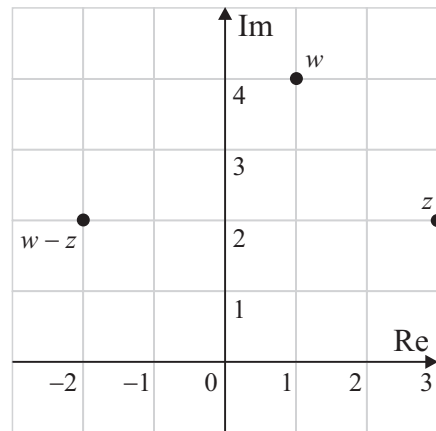
(i) $z = 3 + 2i$

(ii) $w = 1 + 4i$

(iii) $w - z = 1 + 4i - 3 - 2i = -2 + 2i$

Question 2 (b)

$$\begin{aligned} & \frac{1}{5-12i} \quad [\text{Multiply above and below by the conjugate.}] \\ &= \frac{1}{(5-12i)} \times \frac{(5+12i)}{(5+12i)} \quad \boxed{z = a + ib \Rightarrow \bar{z} = a - ib} \\ &= \frac{5+12i}{25+60i-60i-144i^2} \\ &= \frac{5+12i}{25+144} = \frac{5+12i}{169} \\ &= \frac{5}{169} + \frac{12}{169}i \end{aligned}$$



Question 2 (c)

$$\begin{aligned} |k+6i| &= 10 & \boxed{z = a + ib \Rightarrow |z| = \sqrt{a^2 + b^2}} \\ \sqrt{k^2 + 6^2} &= 10 \\ k^2 + 36 &= 100 \\ k^2 &= 64 \\ k &= \pm\sqrt{64} = \pm 8 \end{aligned}$$
