

LC 2015 (SET B): PAPER 1**QUESTION 6 (25 MARKS)****Question 6 (a)**

- (i) **Bank A:** Monthly interest rate $r_M = 0.35\% \Rightarrow i_M = 0.0035$
 $(1 + i_M)^{12} = (1 + i_A)$, where i_A is the annual interest rate
 $(1 + 0.0035)^{12} = (1 + i_A)$
 $(1.0035)^{12} = (1 + i_A)$
 $1.042818 = 1 + i_A$
 $i_A = 0.042818$
 \therefore Annual percentage rate (APR) $r_A = 4.28\%$ [Given to 3 significant figures]
- (ii) **Bank B:** Annual interest rate $r_A = 4.5\% \Rightarrow i_A = 0.045$
 Monthly interest rate: $i_M = ?$, $r_M = ?$
 $(1 + i_M)^{12} = (1 + 0.045)$
 $(1 + i_M)^{12} = (1.045)$
 $i_M = 1.045^{\frac{1}{12}} - 1 = 0.0036748$
 $\therefore r_M = 0.367\%$ [Given to 3 significant figures]

MARKING SCHEME NOTES**Question 6 (a) (i) (ii) [Scale 10C (0, 4, 8, 10)]**

- 4:**
- Correct formula in either part
 - Correct substitution in incorrect formula

- 8:**
- Any one section correct

Note: Rate as 0.367% or 0.00367 gets High Partial.

Question 6 (b)**FORMULAE AND TABLES BOOK**

Financial mathematics: Amortisation - mortgages and loans
 (equal repayments at equal intervals) [page 31]

$$A = P \frac{i(1+i)^t}{(1+i)^t - 1}$$

t = Time period (in years)

i = (Annual) rate of interest expressed as a decimal

A = (Annual) repayment amount

P = Principal

NOTE: The time period can be months or weeks instead of years provided the interest rate is given for that time period.

METHOD 1: Use the amortisation formula

Time period: Months

$$r_M = 0.35\% \Rightarrow i_M = 0.0035$$

$$t = 10 \times 12 = 120 \text{ months}$$

$$P = \text{€}80\,000$$

$$\begin{aligned} A &= P \frac{i(1+i)^t}{(1+i)^t - 1} \\ &= 80\,000 \frac{0.0035(1.0035)^{120}}{(1.0035)^{120} - 1} \\ &= \text{€}817.59 \approx \text{€}818 \end{aligned}$$

METHOD 2: Use a geometric series

$$\frac{A}{1.0035} + \frac{A}{1.0035^2} + \dots + \frac{A}{1.0035^{120}} = 80\,000$$

$$A \left[\frac{1}{1.0035} + \frac{1}{1.0035^2} + \dots + \frac{1}{1.0035^{120}} \right] = 80\,000$$

$$A \left[\frac{\frac{1}{1.0035} \left(1 - \left(\frac{1}{1.0035} \right)^{120} \right)}{1 - \frac{1}{1.0035}} \right] = 80\,000$$

$$\therefore A = \frac{80\,000 \left(1 - \frac{1}{1.0035} \right)}{\frac{1}{1.0035} \left(1 - \left(\frac{1}{1.0035} \right)^{120} \right)} = \text{€}817.59 \approx \text{€}818$$

FORMULAE AND TABLES BOOK
Sequences and series:
Geometric series [page 22]

$$S_n = \frac{a(1-r^n)}{1-r}$$

MARKING SCHEME NOTES

Question 6 (b) [Scale 15C (0, 5, 10, 15)] Note: two solutions

1st solution

5: • Any correct step, i.e. correct formula

10: • Substitution in correct formula

or

2nd solution

5: • Correct equation.

• Listing some terms

• Some substitution

10: • Complete substitution and effort at evaluation.

Note: If A and 80 000 interchanged and remainder of work correct, may get High Partial credit.